

Consideriamo il caso in cui nel vuoto, per semplicità, tutte le derivate rispetto a x e y siano nulle. In questo caso le equazioni di Maxwell si riducono a

$$\begin{aligned} \nabla \times \vec{\mathcal{H}} = \epsilon_0 \frac{\partial \vec{\mathcal{E}}}{\partial t} &\Rightarrow \begin{cases} -\frac{\partial \mathcal{H}_y}{\partial z} = \epsilon_0 \frac{\partial \mathcal{E}_x}{\partial t} \\ \frac{\partial \mathcal{H}_x}{\partial z} = \epsilon_0 \frac{\partial \mathcal{E}_y}{\partial t} \\ 0 = \epsilon_0 \frac{\partial \mathcal{E}_z}{\partial t} \end{cases} \\ -\nabla \times \vec{\mathcal{E}} = \mu_0 \frac{\partial \vec{\mathcal{H}}}{\partial t} &\Rightarrow \begin{cases} \frac{\partial \mathcal{E}_y}{\partial z} = \mu_0 \frac{\partial \mathcal{H}_x}{\partial t} \\ -\frac{\partial \mathcal{E}_x}{\partial z} = \mu_0 \frac{\partial \mathcal{H}_y}{\partial t} \\ 0 = \epsilon_0 \frac{\partial \mathcal{H}_z}{\partial t} \end{cases} \\ \nabla \cdot \vec{\mathcal{E}} = 0 &\Rightarrow \frac{\partial \mathcal{E}_z}{\partial z} \\ \nabla \cdot \vec{\mathcal{H}} = 0 &\Rightarrow \frac{\partial \mathcal{H}_z}{\partial z} \end{aligned}$$

Si possono individuare i seguenti sistemi disaccoppiati di equazioni

$$\text{a) } \begin{cases} -\frac{\partial \mathcal{H}_y}{\partial z} = \epsilon_0 \frac{\partial \mathcal{E}_x}{\partial t} \\ -\frac{\partial \mathcal{E}_x}{\partial z} = \mu_0 \frac{\partial \mathcal{H}_y}{\partial t} \end{cases}$$

$$\text{b) } \begin{cases} \frac{\partial \mathcal{H}_x}{\partial z} = \epsilon_0 \frac{\partial \mathcal{E}_y}{\partial t} \\ \frac{\partial \mathcal{E}_y}{\partial z} = \mu_0 \frac{\partial \mathcal{H}_x}{\partial t} \end{cases}$$

$$\text{c) } \begin{cases} \epsilon_0 \frac{\partial \mathcal{E}_z}{\partial t} = 0 \\ \frac{\partial \mathcal{E}_z}{\partial z} = 0 \end{cases}$$

$$\text{d) } \begin{cases} \mu_0 \frac{\partial \mathcal{H}_z}{\partial t} = 0 \\ \frac{\partial \mathcal{H}_z}{\partial z} = 0 \end{cases}$$